# Package 'SPSP'

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Type Package

Title Selection by Partitioning the Solution Paths

#### Description

An implementation of the feature Selection procedure by Partitioning the entire Solution Paths (namely SPSP) to identify the relevant features rather than using a single tuning parameter. By utilizing the entire solution paths, this procedure can obtain better selection accuracy than the commonly used approach of selecting only one tuning parameter based on existing criteria, cross-validation (CV), generalized CV, AIC, BIC, and extended BIC (Liu, Y., & Wang, P. (2018) <doi:10.1214/18-EJS1434>). It is more stable and accurate (low false positive and false negative rates) than other variable selection approaches. In addition, it can be flexibly coupled with the solution paths of Lasso, adaptive Lasso, ridge regression, and other penalized estimators.

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Maintainer Xiaorui (Jeremy) Zhu <zhuxiaorui1989@gmail.com>

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BugReports https://github.com/XiaoruiZhu/SPSP/issues

License GPL (>= 2) Encoding UTF-8 Depends R (>= 3.5.0) Imports Rcpp (>= 1.0.7), glmnet, ncvreg, Matrix, lars LinkingTo Rcpp Suggests testthat (>= 3.0.0), MASS Config/testthat/edition 3 RoxygenNote 7.2.3 NeedsCompilation yes Author Xiaorui (Jeremy) Zhu [aut, cre], Yang Liu [aut], Peng Wang [aut] Repository CRAN Date/Publication 2023-10-22 17:20:02 UTC

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SPSP-package

Selection by Partitioning the Solution Paths

# Description

An implementation of the feature Selection procedure by Partitioning the entire Solution Paths (namely SPSP) to identify the relevant features rather than using a single tuning parameter. By utilizing the entire solution paths, this procedure can obtain better selection accuracy than the commonly used approach of selecting only one tuning parameter based on existing criteria, cross-validation (CV), generalized CV, AIC, BIC, and EBIC (Liu, Y., & Wang, P. (2018)). It is more stable and accurate (low false positive and false negative rates) than other variable selection approaches. In addition, it can be flexibly coupled with the solution paths of Lasso, adaptive Lasso, ridge regression, and other penalized estimators.

## Details

This package includes two main functions and several functions (fitfun.SP) to obtains the solution paths. The SPSP function allows users to specify the penalized likelihood approaches that will generate the solution paths for the SPSP procedure. Then this function will automatically partitioning the entire solution paths. Its key idea is to classify variables as relevant or irrelevant at each tuning parameter and then to select all of the variables which have been classified as relevant at least once. The SPSP\_step purely apply the partitioning step that needs the solution paths as the input. In addition, there are several functions to obtain the solution paths. They can be used as an input of fitfun.SP argument.

### Author(s)

Xiaorui (Jeremy) Zhu, <zhuxiaorui1989@gmail.com>, Yang Liu, <yliu23@fhcrc.org>, Peng Wang, <wangp9@ucmail.uc.edu>

#### References

Liu, Y., & Wang, P. (2018). Selection by partitioning the solution paths. *Electronic Journal of Statistics*, 12(1), 1988-2017. <10.1214/18-EJS1434>

Fitting-Functions	Four Fitting-Functions that can be used as an input of fitfun. SP ar- gument to obtain the solution paths for the SPSP algorithm. The users can also customize a function to generate the solution paths. As long as the customized function take arguments x, y, family, standardize, and intercept, and return an object of class glmnet, lars (or SCAD, MCP in the future)
	MCP <i>in the future</i> ).

#### Description

Four Fitting-Functions that can be used as an input of fitfun. SP argument to obtain the solution paths for the SPSP algorithm. The users can also customize a function to generate the solution paths. As long as the customized function take arguments x, y, family, standardize, and intercept, and return an object of class glmnet, lars (or SCAD, MCP in the future).

lasso.glmnet uses lasso selection from glmnet.

adalasso.glmnet the function to conduct the adaptive lasso selection using the lambda.1se from cross-validation lasso method to obtain initial coefficients. It uses package glmnet.

adalassoCV.glmnet adaptive lasso selection using the lambda.lse from cross-validation adaptive lasso method to obtain initial coefficients. It uses package glmnet.

ridge.glmnet uses ridge regression to obtain the solution path.

lasso.lars uses lasso selection in lars to obtain the solution path.

SCAD.ncvreg uses SCAD penalty from ncvreg for fitting regularization paths.

MCP.ncvreg uses MCP penalty from ncvreg for fitting regularization paths.

#### Usage

lasso.glmnet(x, y, family, standardize, intercept, ...)
adalasso.glmnet(x, y, family, standardize, intercept, ...)
adalassoCV.glmnet(x, y, family, standardize, intercept, ...)
ridge.glmnet(x, y, family, standardize, intercept, ...)
lasso.lars(x, y, family, standardize, intercept, ...)
SCAD.ncvreg(x, y, family, standardize, intercept, ...)
MCP.ncvreg(x, y, family, standardize, intercept, ...)

#### Arguments

х

a matrix of the independent variables. The dimensions are (nobs) and (nvars); each row is an observation vector.

У	Response variable. Quantitative for family="gaussian" or family="poisson" (non-negative counts). For family="binomial" should be either a factor with two levels.
family	Response type. Either a character string representing one of the built-in families, or else a glm() family object.
standardize	logical argument. Should conduct standardization before the estimation? Default is TRUE.
intercept	logical. If x is a data.frame, this argument determines if the resulting model matrix should contain a separate intercept or not. Default is TRUE.
	Additional optional arguments.

# Value

An object of class "glmnet" is returned to provide solution paths for the SPSP algorithm.

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An object of class "glmnet" is returned to provide solution paths for the SPSP algorithm.

An object of class "glmnet" is returned to provide solution paths for the SPSP algorithm.

An object of class "lars" is returned to provide solution paths for the SPSP algorithm.

An object of class "ncvreg" is returned to provide SCAD penalty solution paths for the SPSP algorithm.

An object of class "ncvreg" is returned to provide solution paths for the SPSP algorithm.

HighDim

A high dimensional dataset with n equals to 200 and p equals to 500.

## Description

A dataset with 200 observations and 500 dimensions is generated from the following process: linear regression model with only first three non-zero coefficients equal to 3, 2, and 1.5 respectively. The covariates are correlated with AR structure (rho=0.3). The error term is normally distributed with zero mean and sd equals to 0.5.

#### Usage

data(HighDim)

# Examples

```
# HighDim dataset is generated from the following process:
n <- 200; p <- 500; sigma <- 0.5
beta <- rep(0, p); nonzero <- c(1, 2, 3); zero <- setdiff(1:p, nonzero)
beta[nonzero] <- c(3, 2, 1.5)
Sigma <- 0.3^(abs(outer(1:p,1:p,"-")))
library(MASS)
X <- mvrnorm(n, rep(0,p), Sigma)</pre>
```

# SPSP

```
error <- rnorm(n, 0, sigma)
X <- apply(X, 2, scale) * sqrt(n)/sqrt(n-1)
error <- error - mean(error)
Y <- X %*% beta + error
HighDim <- data.frame(Y, X)
head(HighDim)</pre>
```

SPSP

Selection by partitioning the solution paths of Lasso, Adaptive Lasso, and Ridge penalized regression.

# Description

A user-friendly function to conduct the selection by Partitioning the Solution Paths (the SPSP algorithm). The user only needs to specify the independent variables matrix, response, family, and fitfun.SP.

# Usage

```
SPSP(
    x,
    y,
    family = c("gaussian", "binomial"),
    fitfun.SP = adalasso.glmnet,
    args.fitfun.SP = list(),
    standardize = TRUE,
    intercept = TRUE,
    ...
)
```

## Arguments

x	A matrix with all independent variables, of dimension n by p; each row is an observation vector with p variables.
У	Response variable. Quantitative for family="gaussian" or family="poisson" (non-negative counts). For family="binomial" should be either a factor with two levels.
family	Response type. Either a character string representing one of the built-in families, or else a glm() family object.
fitfun.SP	A function to obtain the solution paths for the SPSP algorithm. This function takes the arguments x, y, family as above, and additionally the standardize and intercept and others in glmnet, ncvreg, or lars. The function fit the penalized models with lasso, adaptive lasso, SCAD, or MCP penalty, or ridge regression to return the solution path of the corresponding penalized likelihood approach.

	lasso.glmnet lasso selection from glmnet.
	adalasso.glmnet adaptive lasso selection using the lambda.1se from cross- validation lasso method to obtain initial coefficients. It uses package glmnet.
	adalassoCV.glmnet adaptive lasso selection using the lambda.1se from cross- validation adaptive lasso method to obtain initial coefficients. It uses pack- age glmnet.
	ridge.glmnet use ridge regression to obtain the solution path.
	SCAD.ncvreg use SCAD-penalized regression model in ncvreg to obtain the solution path.
	MCP.ncvreg use MCP-penalized regression model in ncvreg to obtain the so- lution path.
	lasso.lars use lasso selection in lars to obtain the solution path.
args.fitfun.SP	A named list containing additional arguments that are passed to the fitting func- tion; see also argument args.fitfun.SP in do.call.
standardize	logical argument. Should conduct standardization before the estimation? Default is TRUE.
intercept	logical. If x is a data.frame, this argument determines if the resulting model matrix should contain a separate intercept or not. Default is TRUE.
	Additional optional arguments.

# Value

An object of class "SPSP" is a list containing at least the following components:

beta_SPSP	the estimated coefficients of SPSP selected model;	
SØ	the estimated relevant sets;	
nonzero	the selected covariates;	
zero	the covariates that are not selected;	
thres	the boundaries for abs(beta);	
R	the sorted adjacent distances;	
intercept	the estimated intercept when intercept == T.	
This object has attribute contains:		

mod.fit	the fitted penalized regression within the input function fitfun.SP;
family	the family of fitted object;
fitfun.SP	the function to obtain the solution paths for the SPSP algorithm;
args.fitfun.SP	a named list containing additional arguments for the function fitfun.SP.

# Examples

```
data(HighDim)
library(glmnet)
# Use the high dimensional dataset (data(HighDim)) to test SPSP+Lasso and SPSP+AdaLasso:
data(HighDim)
```

```
x <- as.matrix(HighDim[,-1])</pre>
y <- HighDim[,1]</pre>
spsp_lasso_1 <- SPSP::SPSP(x = x, y = y, family = "gaussian", fitfun.SP = lasso.glmnet,</pre>
                             init = 1, standardize = FALSE, intercept = FALSE)
head(spsp_lasso_1$nonzero)
head(spsp_lasso_1$beta_SPSP)
spsp_adalasso_5 <- SPSP::SPSP(x = x, y = y, family = "gaussian", fitfun.SP = adalasso.glmnet,</pre>
                                init = 5, standardize = TRUE, intercept = FALSE)
head(spsp_adalasso_5$nonzero)
head(spsp_adalasso_5$beta_SPSP)
```

```
SPSP_step
```

*The selection step with the input of the solution paths.* 

#### Description

A function to select the relevant predictors by partitioning the solution paths (the SPSP algorithm) based on the user provided solution paths BETA.

#### Usage

```
SPSP_step(
 х,
 у,
 family = c("gaussian", "binomial"),
 BETA,
  standardize = TRUE,
  intercept = TRUE,
  init = 1,
 R = NULL,
  . . .
)
```

two levels.

#### Arguments

x	independent variables as a matrix, of dimension nobs x nvars; each row is an observation vector.
У	response variable. Quantitative for family="gaussian" or family="poisson" (non-negative counts). For family="binomial" should be either a factor with

family	either a character string representing one of the built-in families, or else a glm() family object.
BETA	the solution paths obtained from a prespecified fitting step fitfun. SP = lasso.glmnet etc. It must be a p by k matrix, should be thicker and thicker, each column corresponds to a lambda, and lambda gets smaller and smaller. It is the returned coefficient matrix beta from a glmnet object, or a ncvreg object.
standardize	whether need standardization.
intercept	logical. If x is a data.frame, this argument determines if the resulting model matrix should contain a separate intercept or not.
init	initial coefficients, starting from init-th estimator of the solution paths. The default is 1.
R	sorted adjacent distances, default is NULL. Will be calculated inside.
	Additional optional arguments.

# Value

A list containing at least the following components:

beta_SPSP	the estimated coefficients of SPSP selected model;
SØ	the estimated relevant sets;
nonzero	the selected covariates;
zero	the covariates that are not selected;
thres	the boundaries for abs(beta);
R	the sorted adjacent distances;
intercept	the estimated intercept when intercept == T.

This object has attribute contains:

mod.fit	the fitted penalized regression within the input function fitfun.SP;
family	the family of fitted object;
fitfun.SP	the function to obtain the solution paths for the SPSP algorithm;
args.fitfun.SP	a named list containing additional arguments for the function ${\tt fitfun.SP}.$

# Examples

```
data(HighDim)
library(glmnet)
x <- as.matrix(HighDim[,-1])
y <- HighDim[,1]
lasso_fit <- glmnet(x = x, y = y, alpha = 1, intercept = FALSE)
# SPSP+Lasso method
K <- dim(lasso_fit$beta)[2]
LBETA <- as.matrix(lasso_fit$beta)</pre>
```

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